SPEECH DENOISING IN THE WAVEFORM DOMAIN WITH SELF-ATTENTION

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ABSTRACT

In this work, we present CleanUNet, a causal speech denoising model on the raw waveform. The proposed model is based on an encoder-decoder architecture combined with several self-attention blocks to refine its bottleneck representations, which is crucial to obtain good results. The model is optimized through a set of losses defined over both waveform and multi-resolution spectrograms. The proposed method outperforms the state-of-the-art models in terms of denoised speech quality from various objective and subjective evaluation metrics. ¹

Index Terms— Speech denoising, speech enhancement, raw waveform, U-Net, self-attention

1. INTRODUCTION

Speech denoising [1] is the task of removing background noise from recorded speech, while preserving the perceptual quality and intelligibility of speech signals. It has important applications for audio calls, teleconferencing, speech recognition, and hearing aids, thus has been studied over several decades. Traditional signal processing methods, such as spectral subtraction [2] and Wiener filtering [3], are required to produce an estimate of noise spectra and then the clean speech given the additive noise assumption. These methods work well with stationary noise process, but may not generalize well to non-stationary or structured noise types such as dogs barking, baby crying, or traffic horn.

Neural networks have been introduced for speech enhancement since the 1980s [4, 5]. With the increased computation power, deep neural networks (DNN) are often used, e.g., [6, 7]. Over the past years, DNN-based methods for speech enhancement have obtained the state-of-the-art results. The models are usually trained in the supervised setting, where the models learn to predict the clean speech signal given the input noise speech. These methods can be categorized into time-frequency and waveform domain methods. A large body of works are based on time-frequency representations (e.g., STFT) [7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20]. They take the noisy spectral feature (e.g., magnitude of spectrogram,

complex spectrum) as the input, and predict the spectral feature or certain mask for modulation of clean speech (e.g., Ideal Ratio Mask [21]). Then, the waveform is resynthesized given the predicted spectral feature with other extracted information from the input noisy speech (e.g., phase). Another family of speech denoising models directly predict the clean speech waveform from the noisy waveform input [22, 23, 24, 25, 26]. In previous studies, although the waveform methods are conceptually compelling and sometimes preferred in subjective evaluation, they are still lagging behind the time-frequency methods in terms of objective evaluations (e.g., PESQ [27]).

For waveform methods, there are two popular architecture backbones: WaveNet [28] and U-Net [29]. WaveNet can be applied to process the raw waveform [23] as in speech synthesis [30], or low-dimensional embeddings for efficiency reason [31]. U-Net is an encoder-decoder architecture with skip connections tailored for dense prediction, which is particularly suitable for speech denoising [22]. To further improve the denoising quality, different bottleneck layers between the encoder and the decoder are introduced. Examples include dilated convolutions [32, 25], stand-alone WaveNet [24], and LSTM [26]. In addition, several works use the GAN loss to train their models [22, 33, 25, 34].

In this paper, we propose CleanUNet, a causal speech denoising model in the waveform domain. Our model is built on a U-Net structure [29], consisting of an encoder-decoder with skip connections and bottleneck layers. In particular, we use masked self-attentions [35] to refine the bottleneck representation, which is crucial to achieve the state-of-the-art results. Both the encoder and decoder only use causal convolutions, so the overall architectural latency of the model is solely determined by the temporal resampling ratio between the original time-domain waveform and the bottleneck representation (e.g., 16ms for 16kHz audio). We conduct a series of ablation studies on the architecture and loss function, and demonstrate that our model outperforms the state-of-the-art waveform methods in terms of various evaluations.

2. MODEL

2.1. Problem Settings

The goal of this paper is to develop a model that can denoise speech collected from a single channel microphone. The

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¹Audio samples: https://cleanunet.github.io/

model is causal for online streaming applications. Formally, let $x_{\text{noisy}} \in R^T$ be the observed noisy speech waveform of length T. We assume the noisy speech is a mixture of clean speech x and background noise x_{noise} of the same length: $x_{\text{noisy}} = x + x_{\text{noise}}$. The goal is to obtain a denoiser function f such that (1) $\hat{x} = f(x_{\text{noisy}}) \approx x$, and (2) f is causal: the t-th element of the output \hat{x}_t is only a function of previous observations $x_{1:t}$.

2.2. Architecture

We adopt a U-Net architecture [29, 36] for our model f. It contains an encoder, a decoder, and a bottleneck between them. The encoder and decoder have the same number of layers, and are connected via skip connections (identity maps). We visualize the model architecture in Fig. 1.

Encoder. The encoder has D encoder layers, where D is the depth of the encoder. Each encoder layer is composed of a strided 1-d convolution (Conv1d) followed by the rectified linear unit (ReLU) and an 1×1 convolution (Conv1 $\times 1$) followed by the gated linear unit (GLU), similar to [26]. The Conv1d down-samples the input in length and increases the number of channels. The Conv1d in the first layer outputs H channels, where H controls the capacity of the model, and Conv1d's in other layers double the number of channels. Each Conv1d has kernel size K and stride S = K/2. Each Conv1 $\times 1$ doubles the number of channels because GLU halves the channels. All 1-d convolutions are causal.

Decoder. The decoder has D decoder layers. Each decoder layer is paired with the corresponding encoder layer in the reversed order; for instance, the last decoder layer is paired with the first encoder layer. Each pair of encoder and decoder layers are connected via a skip connection. Each decoder layer is composed of a $Conv1 \times 1$ followed by GLU and a transposed 1-d convolution (ConvTranspose1d). The ConvTranspose1d in each decoder layer is causal and has the same hyper-parameters as the Conv1d in the paired encoder layer, except that the number of input and output channels are reversed.

Bottleneck. The bottleneck is composed of N self attention blocks [35]. Each self attention block is composed of a multihead self attention layer and a position-wise fully connected layer. Each layer has a skip connection around it followed by layer normalization. Each multi-head self attention layer has 8 heads, model dimension 512, and the attention map is masked to ensure causality. Each fully connected layer has input channel size 512 and output channel size 2048.

2.3. Loss Function

The loss function has two terms: the ℓ_1 loss on waveform and an STFT loss between clean speech x and denoised speech $\hat{x} = f(x_{\text{noisy}})$. Let $s(x; \theta) = |\text{STFT}(x)|$ be the magnitude of the linear-scale spectrogram of x, where θ represents the hyperparameters of STFT including the hop size, the window length, and the FFT bin. Then, we use multi-resolution STFT [37] as

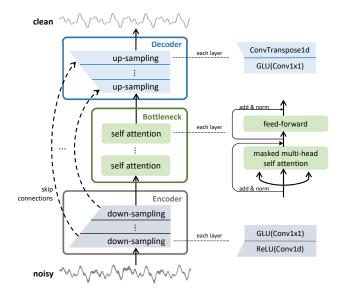


Fig. 1: Model architecture for CleanUNet. It is causal with noisy waveform as input and clean speech waveform as output.

our full-band STFT loss:

$$M-STFT(x,\hat{x}) = \sum_{i=1}^{m} \left(\frac{\|s(x;\theta_i) - s(\hat{x};\theta_i)\|_F}{\|s(x;\theta_i)\|_F} + \frac{1}{T} \left\| \log \frac{s(x;\theta_i)}{s(\hat{x};\theta_i)} \right\|_1 \right), \quad (1)$$

where m is the number of resolutions and θ_i is the STFT parameter for each resolution. Then, our loss function is $\frac{1}{2}M\text{-STFT}(x,\hat{x}) + \|x - \hat{x}\|_1$.

In practice, we find the full-band M-STFT loss sometimes leads to low-frequency noises on the silence part of denoised speech, which deteriorates the human listening test. On the other hand, if our model is trained with ℓ_1 loss only, the silence part of the output is clean, but the high-frequency bands are less accurate than the model trained with the M-STFT loss. This motivated us to define a high-band multi-resolution STFT loss. Let $s_h(x)$ only contains the second half number of rows of s(x) (e.g., 4kHz to 8kHz range of the frequency bands for 16kHz audio). Then, the high-band STFT loss M-STFT $h(x,\hat{x})$ is defined by substituting $s(\cdot)$ with $s_h(\cdot)$ in Eq. (1). Finally, the high-band loss function is $\frac{1}{2}$ M-STFT $h(x,\hat{x}) + \|x - \hat{x}\|_1$.

3. EXPERIMENT

We evaluate the proposed CleanUNet on three datasets: the Deep Noise Suppression (DNS) dataset [38], the Valentini dataset [39], and an internal dataset. We compare our model with the state-of-the-art (SOTA) models in terms of various objective and subjective evaluations. The results are summarized in Tables 1, 2, and 3. We also perform an ablation study for the architecture design and loss function.

Data preparation: For each training data pair (x_{noisy}, x) , we randomly take (aligned) L-second clips for both of them. We

Table 1: Objective and subjective evaluation results for denoising on the DNS no-reverb testset.

Model	Domain	PESQ (WB)	PESQ (NB)	STOI (%)	pred. CSIG	pred. CBAK	pred. COVRL	MOS SIG	MOS BAK	MOS OVRL
Noisy dataset	-	1.585	2.164	91.6	3.190	2.533	2.353	-	-	-
DTLN [19]	Time-Freq	-	3.04	94.8	-	-	-	-	-	-
PoCoNet [20]	Time-Freq	2.745	-	-	4.080	3.040	3.422	-	-	-
FullSubNet [18]	Time-Freq	2.897	3.374	96.4	4.278	3.644	3.607	3.97	3.72	3.75
Conv-TasNet [31]	Waveform	2.73	-	-	-	-	-	-	-	-
FAIR-denoiser [26]	Waveform	2.659	3.229	96.6	4.145	3.627	3.419	3.68	4.10	3.72
CleanUNet ($N = 5$, ℓ_1 +full)	Waveform	3.146	3.551	97.7	4.619	3.892	3.932	4.03	3.89	3.78
CleanUNet ($N = 5$, ℓ_1 +high)	Waveform	3.011	3.460	97.3	4.513	3.812	3.800	3.94	4.08	3.87

Table 2: Objective evaluation results for denoising on the Valentini test dataset.

Model	Domain	PESQ (WB)	PESQ (NB)	STOI (%)	pred. CSIG	pred. CBAK	pred. COVRL
Noisy dataset	-	1.943	2.553	92.7	3.185	2.475	2.536
FAIR-denoiser [26]	Waveform	2.835	3.329	95.3	4.269	3.377	3.571
CleanUNet $(N = 3, \ell_1 + \text{full})$	Waveform	2.884	3.396	95.5	4.317	3.406	3.625
CleanUNet ($N = 5, \ell_1$ +full)	Waveform	2.905	3.408	95.6	4.338	3.422	3.645

Table 3: Objective evaluation results for denoising on the internal test dataset.

Model	Domain	PESQ (WB)	PESQ (NB)	STOI (%)	pred. CSIG	pred. CBAK	pred. COVRL
Noisy dataset	-	1.488	1.861	86.2	2.436	2.398	1.927
FullSubNet [18]	Time-Freq	2.442	2.908	92.0	3.650	3.369	3.046
Conv-TasNet [31]	Waveform	1.927	2.349	92.2	2.869	2.004	2.388
FAIR-denoiser [26]	Waveform	2.087	2.490	92.8	3.120	3.173	2.593
CleanUNet ($N = 5, \ell_1$ +full)	Waveform	2.450	2.915	93.8	3.981	3.423	3.270
CleanUNet ($N = 5$, ℓ_1 +high)	Waveform	2.387	2.833	93.3	3.905	3.347	3.151

then apply various data augmentation methods to these clips, which we will specify for each dataset.

Architecture: The depth of the encoder or the decoder is D=8. Each encoder/decoder layer has hidden dimension H=48 or 64, stride S=2, and kernel size K=4. The depth of the bottleneck is N=3 or 5. Each self attention block has 8 heads, model dimension =512, middle dimension =2048, no dropout and no positional encoding.

Optimization: We use the Adam optimizer with momentum $\beta_1=0.9$ and denominator momentum $\beta_2=0.999$. We use the linear warmup with cosine annealing learning rate schedule with maximum learning rate 2×10^{-4} and warmup ratio =5%. We survey three kinds of losses: (1) ℓ_1 loss on waveform, (2) ℓ_1 loss + full-band STFT, (3) ℓ_1 loss + high-band STFT described in Section 2.3. All models are trained on 8 NVIDIA V100 GPUs.

Evaluation: We conduct both objective and subjective evaluations for denoised speech. Objective evaluation methods include (1) Perceptual Evaluation of Speech Quality (PESQ [27]), (2) Short-Time Objective Intelligibility (STOI [40]), and (3) Mean Opinion Score (MOS) prediction of the *i*) distortion of speech signal (SIG), *ii*) intrusiveness of background noise (BAK), and *iii*) overall quality (OVRL) [41]. For subjective

evaluation, we perform a MOS test as recommended in ITU-T P.835 [42]. We launched a crowd source evaluation on Mechanical Turk. We randomly select 100 utterances from the test set, and each utterance is scored by 15 workers along three axis: SIG, BAK, and OVRL.

3.1. DNS

The DNS dataset [38] contains recordings of more than 10K speakers reading 10K books with a sampling rate 16kHz. We synthesize 500 hours of clean & noisy speech pairs with 31 SNR levels (-5 to 25 dB) to create the training set [38]. We set the clip L=10. We then apply the RevEcho augmentation [26] (which adds decaying echoes) to the training data.

We compare the proposed CleanUNet with several SOTA models on DNS. By default, FAIR-denoiser [26] only use ℓ_1 waveform loss on DNS dataset for better subjective evaluation. We use hidden dimension H=64. We study both full and high-band STFT losses as described in Section 2.3 with multi-resolution hop sizes in $\{50,120,240\}$, window lengths in $\{240,600,1200\}$, and FFT bins in $\{512,1024,2048\}$. We train the models for 1M iterations with a batch size of 16. We report the objective and subjective evaluations on the no-reverb testset in Table 1. CleanUNet outperforms all baselines in

Table 4: Objective evaluation results for the ablation study of CleanUNet on the DNS no-reverb testset.

\overline{N}	loss	PESQ (WB)	PESQ (NB)	STOI (%)
	ℓ_1	2.750	3.319	96.9
3	ℓ_1 + full	3.128	3.539	97.6
	ℓ_1 + high	3.006	3.453	97.3
	ℓ_1	2.797	3.362	97.0
5	ℓ_1 + full	3.146	3.551	97.7
3	ℓ_1 + high	3.011	3.460	97.3

Table 5: Objective evaluation results for the ablation study of architecture on the DNS no-reverb testset. Stride is S = K/2. RS means resampling using sinc interpolation [43]. All models downsample 16khz audio $256 \times$ for bottleneck representation.

Model	D	K	RS	PESQ (WB)	PESQ (NB)	STOI (%)
FAIR-denoiser	5	8	yes	2.849	3.329	96.9
CleanUNet	5	8	yes	3.024	3.459	97.3
CleanUNet	4	8	no	2.982	3.425	97.2
CleanUNet	8	4	no	3.146	3.551	97.7

objective evaluations. For MOS evaluations, it get the highest SIG and OVRL, and slightly lower BAK.

Ablation Studies: We perform ablation study to investigate the hyper-parameters and loss functions in our model. We survey N=3 or 5 self attention blocks in the bottleneck. We also survey different combination of loss terms. The objective evaluation results are in Table 4. Full-band STFT loss and N=5 consistently outperforms the others in terms of objective evaluations.

In order to show the importance of each component in CleanUNet, we perform an ablation study by gradually replacing the components in FAIR-denoiser [26] to our model in Table 5. First, we train FAIR-denoiser with the full-band STFT loss. The architecture has D=5 (kernel size K=8 and stride S=4), a resampling layer (realized by the sinc interpolation filter [43]), and LSTM as the bottleneck. Next, we replace the LSTM with N=5 self attention blocks, which leads to a boost of PESQ score from 2.849 to 3.024. We then remove the sinc resampling operation and reduce the depth of the encoder/decoder to D=4, which only has minor impact. Finally, we double the depth to D=8 and reduce the kernel size to K=4 and stride to S=2, which significantly improves the results. Note that all these models produce the same length of bottleneck representation.

Inference Speed and Model Footprints: We compare the inference speed and model footprints between the FAIR-denoiser and CleanUNet. We use hidden dimension H=64 in all models. The inference speed is measured in terms of the real time factor (RTF), which is the time required to generate certain speech divided by the total time of the speech. We use a batch-size of 4 and length L=10 seconds under a sampling rate

Table 6: Inference speed (RTF) and model footprints (#/ parameters) of the FAIR-denoiser and CleanUNet. The algorithmic latency for all models is 16ms for 16khz audio.

Model	RTF	Footprint
FAIR-denoiser	2.59×10^{-3} 3.19×10^{-3}	33.53M
CleanUNet $(N = 3)$	3.19×10^{-3}	39.77M
CleanUNet $(N=5)$	3.43×10^{-3}	46.07M

16kHz. The results are reported in Table 6.

3.2. Valentini

The Valentini dataset [39] contains 28.4 hours of clean & noisy speech pairs collected from 84 speakers with a sampling rate 48kHz. There are 4 SNR levels (0, 5, 10, and 15 dB). At each iteration, we randomly select L to be a real value between 1.33 and 1.5. We then apply the Remix augmentation (which shuffles noises within a local batch) and the BandMask augmentation [26] (which removes a fraction of frequencies) to the training data. We compare our CleanUNet with FAIR-denoiser [26] as the baseline. In both models we use hidden dimension H=48 and the full-band STFT loss with the same setup as DNS dataset. We train the models for 1M iterations with a batch size of 64. We report the objective evaluation results in Table 2. Our model consistently outperforms FAIR-denoiser in all metrics.

3.3. Internal Dataset

We also conduct experiments on an challenging internal dataset. The dataset contains 100 hours of clean & noisy speech with a sampling rate 48kHz. Each clean audio may contain speech from multiple speakers. We use the same data preparation (L=10) and augmentation method as the DNS dataset in Section 3.1.

We compare the proposed CleanUNet with FAIR-denoiser and FullSubNet on this internal dataset. We set H=64, N=5, D=8, K=8, S=2. We use full and high-band STFT losses with the same setup as DNS dataset. We train the models for 1M iterations with a batch size of 16. We report the objective evaluation results in Table 3. Our model consistently outperforms FullSubNet and FAIR-denoiser in all metrics.

4. CONCLUSION

In this paper, we introduce CleanUNet, a causal speech denoising model in the waveform domain. Our model uses the U-Net like encoder-decoder as the backbone, and relies on self-attention modules to refine its bottleneck representation. We test our model on various datasets, and show that it achieves the state-of-the-art performance in terms of objective and subjective evaluation metrics in the speech denoising task. We also conduct a series of ablation studies for architecture design choices and different combinations of loss functions.

5. REFERENCES

- [1] Philipos C Loizou, *Speech enhancement: theory and practice*, CRC press, 2007.
- [2] Steven Boll, "Suppression of acoustic noise in speech using spectral subtraction," *IEEE Transactions on acoustics, speech, and signal processing*, 1979.
- [3] Jae Soo Lim and Alan V Oppenheim, "Enhancement and bandwidth compression of noisy speech," *Proceedings of the IEEE*, vol. 67, no. 12, pp. 1586–1604, 1979.
- [4] Shinichi Tamura and Alex Waibel, "Noise reduction using connectionist models," in *ICASSP*. IEEE, 1988.
- [5] Shahla Parveen and Phil Green, "Speech enhancement with missing data techniques using recurrent neural networks," in ICASSP, 2004.
- [6] Xugang Lu et al., "Speech enhancement based on deep denoising autoencoder.," in *Interspeech*, 2013.
- [7] Yong Xu et al., "A regression approach to speech enhancement based on deep neural networks," *IEEE/ACM Transactions on Audio, Speech, and Language Processing*, 2014.
- [8] Meet Soni et al., "Time-frequency masking-based speech enhancement using generative adversarial network," in *ICASSP*, 2018.
- [9] Szu-Wei Fu et al., "MetricGAN: Generative adversarial networks based black-box metric scores optimization for speech enhancement," in *ICML*, 2019.
- [10] Szu-Wei Fu et al., "MetricGAN+: An improved version of metricgan for speech enhancement," arXiv, 2021.
- [11] Yuxuan Wang and DeLiang Wang, "A deep neural network for time-domain signal reconstruction," in ICASSP, 2015.
- [12] Felix Weninger et al., "Speech enhancement with 1stm recurrent neural networks and its application to noise-robust asr," in *International conference on latent variable analysis and signal separation*, 2015.
- [13] Aaron Nicolson and Kuldip K Paliwal, "Deep learning for minimum mean-square error approaches to speech enhancement," *Speech Communication*, 2019.
- [14] Francois G Germain et al., "Speech denoising with deep feature losses," *arXiv*, 2018.
- [15] Yong Xu et al., "Multi-objective learning and mask-based post-processing for deep neural network based speech enhancement," *arXiv*, 2017.
- [16] Felix Weninger et al., "Discriminatively trained recurrent neural networks for single-channel speech separation," in *GlobalSIP*, 2014.
- [17] Yangyang Xia et al., "Weighted speech distortion losses for neural-network-based real-time speech enhancement," in ICASSP, 2020.
- [18] Xiang Hao et al., "Fullsubnet: A full-band and sub-band fusion model for real-time single-channel speech enhancement," in ICASSP, 2021.
- [19] Nils Westhausen and Bernd Meyer, "Dual-signal transformation lstm network for real-time noise suppression," *arXiv*, 2020.

- [20] Umut Isik et al., "Poconet: Better speech enhancement with frequency-positional embeddings, semi-supervised conversational data, and biased loss," arXiv, 2020.
- [21] Donald S Williamson et al., "Complex ratio masking for monaural speech separation," *IEEE/ACM transactions on audio, speech, and language processing*, 2015.
- [22] Santiago Pascual et al., "Segan: Speech enhancement generative adversarial network," *arXiv*, 2017.
- [23] Dario Rethage et al., "A wavenet for speech denoising," in ICASSP, 2018.
- [24] Ashutosh Pandey and DeLiang Wang, "TCNN: Temporal convolutional neural network for real-time speech enhancement in the time domain," in *ICASSP*, 2019.
- [25] Xiang Hao et al., "UNetGAN: A robust speech enhancement approach in time domain for extremely low signal-to-noise ratio condition," in *Interspeech*, 2019.
- [26] Alexandre Defossez et al., "Real time speech enhancement in the waveform domain," in *Interspeech*, 2020.
- [27] ITU-T Recommendation, "Perceptual evaluation of speech quality (pesq): An objective method for end-to-end speech quality assessment of narrow-band telephone networks and speech codecs," *Rec. ITU-T P. 862*, 2001.
- [28] Aaron van den Oord et al., "WaveNet: A generative model for raw audio," arXiv, 2016.
- [29] Olaf Ronneberger et al., "U-Net: Convolutional networks for biomedical image segmentation," in *MICCAI*, 2015.
- [30] Wei Ping, Kainan Peng, and Jitong Chen, "ClariNet: Parallel wave generation in end-to-end text-to-speech," in *ICLR*, 2019.
- [31] Yi Luo and Nima Mesgarani, "Conv-tasnet: Surpassing ideal time–frequency magnitude masking for speech separation," *IEEE/ACM transactions on audio, speech, and language processing*, 2019.
- [32] Daniel Stoller et al., "Wave-U-Net: A multi-scale neural network for end-to-end audio source separation," *arXiv*, 2018.
- [33] Deepak Baby and Sarah Verhulst, "Sergan: Speech enhancement using relativistic generative adversarial networks with gradient penalty," in *ICASSP*, 2019.
- [34] Huy Phan et al., "Improving gans for speech enhancement," *IEEE Signal Processing Letters*, 2020.
- [35] Ashish Vaswani et al., "Attention is all you need," in NIPS, 2017.
- [36] Olivier Petit et al., "U-Net Transformer: Self and cross attention for medical image segmentation," in *International Workshop on Machine Learning in Medical Imaging*, 2021.
- [37] Ryuichi Yamamoto et al., "Parallel WaveGAN: A fast waveform generation model based on generative adversarial networks with multi-resolution spectrogram," in *ICASSP*, 2020.
- [38] Chandan KA Reddy et al., "The interspeech 2020 deep noise suppression challenge: Datasets, subjective testing framework, and challenge results," *arXiv*, 2020.
- [39] Cassia Valentini-Botinhao, "Noisy speech database for training speech enhancement algorithms and tts models," 2017.
- [40] Cees H Taal et al., "An algorithm for intelligibility prediction of time–frequency weighted noisy speech," *IEEE Transactions on Audio, Speech, and Language Processing*, 2011.

- [41] Yi Hu and Philipos C. Loizou, "Evaluation of objective quality measures for speech enhancement," *IEEE Transactions on Audio, Speech, and Language Processing*, 2008.
- [42] ITUT Recommendation, "Subjective test methodology for evaluating speech communication systems that include noise suppression algorithm," *ITU-T recommendation*, 2003.
- [43] Julius Smith and Phil Gossett, "A flexible sampling-rate conversion method," in *ICASSP*, 1984.